

**CORRIGENDUM**  
**PARITY OF CLASS NUMBERS AND WITT EQUIVALENCE**  
**OF QUARTIC FIELDS**  
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STANISLAV JAKUBEC, FRANTIŠEK MARKO, AND KAZIMIERZ SZYMICZEK

The proof of the Proposition on p. 1712 incorrectly interprets the nondegeneracy of the Hilbert symbol. Here is the Proposition with corrected proof.

**Proposition.** *Let  $F$  be a number field such that  $s(F) = 2$  and  $s_1 = \cdots = s_g = 1$ . Then the class number of  $F$  is even, and every number field Witt equivalent to  $F$  has also even class number.*

*Proof.* Take a nondyadic prime  $\mathfrak{q}$  of  $F$  with  $s(F_{\mathfrak{q}}) = 2$  (there must be one since  $s(F) = 2$ ). We show that the order  $d$  of the ideal class  $[\mathfrak{q}]$  in the ideal class group of  $F$  is even. For suppose  $d$  is odd. Then  $\mathfrak{q}^d = (a)$  is a principal ideal and the number  $a$  is a  $\mathfrak{q}$ -adic prime times a  $\mathfrak{q}$ -adic square. Since  $-1$  is not a local square at  $\mathfrak{q}$ , we have  $(-1, a)_{\mathfrak{q}} = -1$ . On the other hand, we claim that

$$(-1, a)_{\mathfrak{p}} = 1$$

for all the remaining primes  $\mathfrak{p}$  of  $F$ . For a dyadic prime  $\mathfrak{p}$  this is obvious since  $-1$  is a local square at  $\mathfrak{p}$  (the local dyadic levels are all equal to 1). When  $\mathfrak{p}$  is a finite nondyadic prime and  $\mathfrak{p} \neq \mathfrak{q}$ , then  $a$  is a local unit at  $\mathfrak{p}$  (by our choice of  $a$ ), hence again the Hilbert symbol is trivial. Since  $s(F) = 2$ , there are no real infinite primes, and at complex infinite primes any Hilbert symbol is trivial. This proves our claim, contradicting Hilbert reciprocity law. Hence  $d$  must be even, and so also the ideal class number of  $F$  is even.

If  $K$  is any number field Witt equivalent to  $F$ , then  $K$  and  $F$  have the same Witt equivalence invariant. Hence, if  $F$  satisfies Conner's level conditions, so does  $K$ , and, as has been already proved, it has even class number.  $\square$

We take this opportunity to give more precise information about cubic number fields. We have mentioned in the paper that every cubic field is Witt equivalent to a field with odd class number. It is a fact that the representatives of the eight cubic Witt equivalence classes discussed in the paper all have class number one. Thus every cubic field is Witt equivalent to a field with class number one.